## Tuesday 9 June 2015 - Morning

## AS GCE MATHEMATICS

## 4728/01 Mechanics 1

## QUESTION PAPER

Candidates answer on the Printed Answer Book.
OCR supplied materials:

- Printed Answer Book 4728/01
- List of Formulae (MF1)

Other materials required:

- Scientific or graphical calculator

Duration: 1 hour 30 minutes

## INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found inside the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- Write your answer to each question in the space provided in the Printed Answer Book. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer all the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by $\mathrm{g} \mathrm{ms}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g=9.8$.


## INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [ ] at the end of each question or part question on the Question Paper.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- The Printed Answer Book consists of $\mathbf{1 2}$ pages. The Question Paper consists of $\mathbf{4}$ pages. Any blank pages are indicated.


## INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

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1 A particle $P$ is projected vertically downwards with speed $14 \mathrm{~m} \mathrm{~s}^{-1}$ from a point 30 m above the ground.
(i) Calculate the speed of $P$ when it reaches the ground.
(ii) Find the distance travelled by $P$ in the first 0.4 s of its motion.
(iii) Calculate the time taken for $P$ to travel the final 15 m of its descent.


Three particles $P, Q$ and $R$ with masses $0.4 \mathrm{~kg}, 0.3 \mathrm{~kg}$ and $m \mathrm{~kg}$ are moving along the same straight line on a smooth horizontal surface. $P$ and $Q$ are moving towards each other with speeds $u \mathrm{~m} \mathrm{~s}^{-1}$ and $8 \mathrm{~m} \mathrm{~s}^{-1}$ respectively. $R$ has speed $3 \mathrm{~m} \mathrm{~s}^{-1}$ and is moving in the same direction as $Q$ (see diagram).
(i) Immediately after the collision between $P$ and $Q$ their directions of motion have been reversed, but their speeds are unchanged. Calculate $u$.

The next collision is between $Q$ and $R$. After the collision between $Q$ and $R$, particle $Q$ is at rest and $R$ has speed $9 \mathrm{~ms}^{-1}$.
(ii) Calculate $m$.


Two travellers $A$ and $B$ make the same journey on a long straight road. Each traveller walks for part of the journey and rides a bicycle for part of the journey. They start their journeys at the same instant, and they end their journeys simultaneously after travelling for $T$ hours. $A$ starts the journey cycling at a steady $20 \mathrm{~km} \mathrm{~h}^{-1}$ for 1 hour. $A$ then leaves the bicycle at the side of the road, and completes the journey walking at $5 \mathrm{kmh}^{-1}$. $B$ begins the journey walking at a steady $4 \mathrm{~km} \mathrm{~h}^{-1}$. When $B$ finds the bicycle where $A$ left it, $B$ cycles at $15 \mathrm{kmh}^{-1}$ to complete the journey (see diagram).
(i) Calculate the distance $A$ cycles, and hence find the period of time for which $B$ walks before finding the bicycle.
(ii) Find $T$.
(iii) Calculate the distance $A$ and $B$ each travel.


Two forces of magnitudes 6 N and 10 N separated by an angle of $110^{\circ}$ act on a particle $P$, which rests on a horizontal surface (see diagram).
(i) Find the magnitude of the resultant of the 6 N and 10 N forces, and the angle between the resultant and the 10 N force.

The two forces act in the same vertical plane. The particle $P$ has weight 20 N and rests in equilibrium on the surface. Given that the surface is smooth, find
(ii) the magnitude of the force exerted on $P$ by the surface,
(iii) the angle between the surface and the 10 N force.

5 A particle $P$ of mass 0.4 kg is at rest on a horizontal surface. The coefficient of friction between $P$ and the surface is 0.2 . A force of magnitude 1.2 N acting at an angle of $\theta^{\circ}$ above the horizontal is then applied to $P$. Find the acceleration of $P$ in each of the following cases:
(i) $\theta=0$;
(ii) $\theta=20$;
(iii) $\theta=70$;
(iv) $\theta=90$.

6 A particle $P$ moves in a straight line on a horizontal surface. $P$ passes through a fixed point $O$ on the line with velocity $2 \mathrm{~m} \mathrm{~s}^{-1}$. At time $t \mathrm{~s}$ after passing through $O$, the acceleration of $P$ is $(4+12 t) \mathrm{m} \mathrm{s}^{-2}$.
(i) Calculate the velocity of $P$ when $t=3$.
(ii) Find the distance $O P$ when $t=3$.

A second particle $Q$, having the same mass as $P$, moves along the same straight line. The displacement of $Q$ from $O$ is $\left(k-2 t^{3}\right) \mathrm{m}$, where $k$ is a constant. When $t=3$ the particles collide and coalesce.
(iii) Find the value of $k$.
(iv) Find the common velocity of the particles immediately after their collision.

## Question 7 begins on page 4.


$A B$ and $B C$ are lines of greatest slope on a fixed triangular prism, and $M$ is the mid-point of $B C . A B$ and $B C$ are inclined at $30^{\circ}$ to the horizontal. The surface of the prism is smooth between $A$ and $B$, and between $B$ and $M$. Between $M$ and $C$ the surface of the prism is rough. A small smooth pulley is fixed to the prism at $B$. A light inextensible string passes over the pulley. Particle $P$ of mass 0.3 kg is fixed to one end of the string, and is placed at $A$. Particle $Q$ of mass 0.4 kg is fixed to the other end of the string and is placed next to the pulley on $B C$. The particles are released from rest with the string taut. $P$ begins to move towards the pulley, and $Q$ begins to move towards $M$ (see diagram).
(i) Show that the initial acceleration of the particles is $0.7 \mathrm{~m} \mathrm{~s}^{-2}$, and find the tension in the string.

The particle $Q$ reaches $M 1.8 \mathrm{~s}$ after being released from rest.
(ii) Find the speed of the particles when $Q$ reaches $M$.

After $Q$ passes through $M$, the string remains taut and the particles decelerate uniformly. $Q$ comes to rest between $M$ and $C 1.4 \mathrm{~s}$ after passing through $M$.
(iii) Find the deceleration of the particles while $Q$ is moving from $M$ towards $C$.
(iv) (a) By considering the motion of $P$, find the tension in the string while $Q$ is moving from $M$ towards $C$.
(b) Calculate the magnitude of the frictional force which acts on $Q$ while it is moving from $M$ towards $C$.

## END OF QUESTION PAPER

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